General Instructions

1. All questions are compulsory. There are 26 questions in all.

2. This question paper has five sections: Section A, Section B, Section C, Section D and Section E.

3. Section A contains five questions of one mark each, Section B contains five questions of two marks each, Section C contains twelve questions of three marks each, Section D contains one value based question of four marks and Section E contains three questions of five marks each.

4. There is no overall choice. However, an internal choice has been provided in one question of two marks, one question of three marks and all the three questions of five marks weightage. You have to attempt only one of the choices in such questions.

5. You may use the following values of physical constants wherever necessary.

\[ c = 3 \times 10^8 \text{ m/s} \]

\[ h = 6.63 \times 10^{-34} \text{ Js} \]

\[ e = 1.6 \times 10^{-19} \text{ C} \]

\[ \mu_0 = 4\pi \times 10^{-7} \text{ T m A}^{-1} \]

\[ \varepsilon_0 = 8.854 \times 10^{-12} \text{ C}^2 \text{ N}^{-1} \text{ m}^{-2} \]

\[ \frac{1}{4\pi\varepsilon_0} = 9 \times 10^9 \text{ N m}^2 \text{ C}^{-2} \]

\[ m_e = 9.1 \times 10^{-31} \text{ kg} \]
mass of neutron = $1.675 \times 10^{-27}$ kg

mass of proton = $1.673 \times 10^{-27}$ kg

Avogadro’s number = $6.023 \times 10^{23}$ per gram mole

Boltzmann constant = $1.38 \times 10^{-23}$ JK$^{-1}$

**Section A**

1. What is the value of the angle between the vectors $\vec{p}$ and $\vec{E}$ for which the potential energy of an electric dipole of dipole moment $\vec{p}$, kept in an external electric field $\vec{E}$, has maximum value.

2. Name the colours corresponding to the digits 4 and 7 in the colour code scheme for carbon resistors.

3. State which of the two, the capacitor or an inductor, tends to become a SHORT when the frequency of the applied alternating voltage has a very high value.

4. Redraw the diagram given below and mark the position of the centre of curvature of the spherical mirror used in the given set up.

5. In the given diagram $C(t)$ stands for the carrier wave and $m(t)$ for the signal to be transmitted. What name do we give to the wave labeled as $C_m(t)$ in the diagram?
Section B

6. Calculate the value of the unknown potential V for the given potentiometer circuit. The total length (400 cm) of the potentiometer wire has a resistance of 10 Ω and the balance point is obtained at a length of 240 cm.

7. Name the phenomenon which proves transverse wave nature of light. Give two uses of the devices whose functioning is based on this phenomenon.

OR

Name the phenomenon which is responsible for bending of light around sharp corners of an obstacle. Under what conditions does this phenomenon take place? Give one application of this phenomenon in everyday life.
8. The equivalent wavelength of a moving electron has the same value as that of a photon having an energy of $6 \times 10^{-17}$ J. Calculate the momentum of the electron.

9. The short wavelength limit for the Lyman series of the hydrogen spectrum is 913.4 Å. Calculate the short wavelength limit for Balmer series of hydrogen spectrum.

10. (a) Arrange the following networks in increasing order of the number of computers that may be present in the network:

   Internet ; LAN ; WAN

(b) What is the minimum number of satellites that enables a Global Positioning System (GPS) receiver to determine one’s longitude/latitude position, i.e., to make a 2D position fix.

Section C

11. Eight identical spherical drops, each carrying a charge $1 \text{ nC}$ are at a potential of 900 V each. All these drops combine together to form a single large drop. Calculate the potential of this large drop. (Assume no wastage of any kind and take the capacitance of a sphere of radius $r$ as proportional to $r$).

12. The current flowing in the galvanometer G when the key $k_2$ is kept open is $I$. On closing the key $k_2$, the current in the galvanometer becomes $I/n$, where $n$ is an integer. Obtain an expression for resistance $R_g$ of the galvanometer in terms of $R$, $S$ and $n$. To what form does this expression reduce when the value of $R$ is very large as compared to $S$?
13. The magnitude $F$ of the force between two straight parallel current carrying conductors kept at a distance $d$ apart in air is given by

$$F = \frac{\mu_0 I_1 I_2}{2\pi d}$$

Where $I_1$ and $I_2$ are the currents flowing through the two wires

Use this expression, and the sign convention that the:

“Force of attraction is assigned a negative sign and Force of repulsion is assigned a positive sign”.

Draw graphs showing dependence of $F$ on

(i) $I_1 I_2$ when $d$ is kept constant
(ii) $d$ when the product $I_1 I_2$ is maintained at a constant positive value.
(iii) $d$ when the product $I_1 I_2$ is maintained at a constant negative value.

OR

The given graphs show the variation of intensity of magnetization $I$ with strength of applied magnetic field $H$ for two magnetic materials P and Q.
(i) Identify the materials P and Q.

(ii) For material P, plot the variation of Intensity of Magnetisation with temperature. Justify your answer.

14. Find the value of the phase lag/lead between the current and voltage in the given series LCR circuit. Without making any other change, find the value of the additional capacitor, such that when ‘suitably joined’ to the capacitor (C = 2\mu F) as shown, would make the power factor of this circuit unity.

15. Explain how one ‘observes an inconsistency’ when Ampere’s circuital law is applied to the process of charging a capacitor.

How this ‘contradiction’ gets removed by introducing the concept of an ‘additional current’, known as the ‘displacement current’?

16. A point object O is kept at a distance of 30 cm from a convex lens of power +4D towards its left. It is observed that when a convex mirror is kept on the right side at a distance of 50 cm from the convex lens, the image of the object O formed by the lens-mirror combination coincides with the object itself.

Calculate the focal length of the convex mirror.
17. The arrangement used by Thomas Young to produce an interference pattern is shown in the given diagram. Justify why there would be no change in the ‘fringe width’ when the main illuminated slit (S) is shifted to the position $S'$ as shown.

18. A given number of atoms $N_0$ of a radioactive element with a half life $T$ is uniformly distributed in the blood stream of a normal person A having total volume $V$ of blood in the body (i) and person B in need of blood transfusion having a volume $V'$ of blood in the body (ii). The number of radioactive atoms per unit volume in the blood streams of the two persons after a time $nT$ are found to be $N_1$ and $N_2$. Prove mathematically that the additional volume of blood that needs to be transfused in the body of person B equals $(\frac{N_2 - N_1}{N_2}) V$

19. A student has to use an appropriate number of (i) NAND gates (only) to get the output $Y_1$ (ii) NOR gates (only) to get the output $Y_2$ From two given inputs A and B as shown in the diagram.
Identify the ‘equivalent gate’ needed in each case. Show how one can connect an appropriate number of (i) NAND (ii) NOR gates respectively in the two cases to get these ‘equivalent gates’.

20. The data given below gives the photon energy (in eV) for a number of waves whose wavelength values (in nm) are also given.

<table>
<thead>
<tr>
<th>Wavelength (in nm)</th>
<th>200</th>
<th>400</th>
<th>600</th>
<th>800</th>
<th>1000</th>
<th>1200</th>
</tr>
</thead>
<tbody>
<tr>
<td>Photon Energy (in eV)</td>
<td>6.216</td>
<td>3.108</td>
<td>2.072</td>
<td>1.554</td>
<td>1.243</td>
<td>1.036</td>
</tr>
</tbody>
</table>

(Without doing any calculation/taking any reading), explain how one can use this data to draw an appropriate graph to infer

(i) photon energy corresponding to a wavelength of 100 nm.
(ii) the wavelength value (in nm) corresponding to a photon energy of 1 eV.
(iii) velocity of light assuming that the value of Plank’s constant is known.

21. A (sinusoidal) carrier wave

\[ C(t) = A_C \sin \omega_c t \]
is amplitude modulated by a (sinusoidal) message signal

\[ m(t) = A_m \sin \omega_m t \]

Write the equation of the (amplitude) modulated signal. Use this equation to obtain the values of the frequencies of all the sinusoidal waves present in the modulated signal.

22. Give reasons for the following:

(i) The Zener diode is fabricated by heavily doping both the p and n sides of the junction
(ii) A photodiode, when used as a detector of optical signals is operated under reverse bias.
(iii) The band gap of the semiconductor used for fabrication of visible LED’s must at least be 1.8 eV.

**Section D**

23. Dimpi’s class was shown a video on effects of magnetic field on a current carrying straight conductor. She noticed that the force on the straight current carrying conductor becomes zero when it is oriented parallel to the magnetic field and this force becomes maximum when it is perpendicular to the field. She shared this interesting information with her grandfather in the evening. The grandfather could immediately relate it to something similar in real life situations. He explained it to Dimpi that similar things happen in real life too. When we align and orient our thinking and actions in an adaptive and accommodating way, our lives become more peaceful and happy. However, when we adopt an unaccommodating and stubborn attitude, life becomes troubled and miserable. We should therefore always be careful in our response to different situations in life and avoid unnecessary conflicts.

Answer the following question based on above information:

a) Express the force acting on a straight current carrying conductor kept in a magnetic field in vector form. State the rule used to find the direction of this force.

b) Which one value is displayed and conveyed by grandfather as well as Dimpi?

c) Mention one specific situation from your own life which reflects similar values shown by you towards your elders.
**Section E**

24 a) State the theorem which relates total charge enclosed within a closed surface and the electric flux passing through it. Prove it for a single point charge.

b) An ‘atom’ was earlier assumed to be a sphere of radius a having a positively charged point nucleus of charge $+Ze$ at its centre. This nucleus was believed to be surrounded by a uniform density of negative charge that made the atom neutral as a whole.

Use this theorem to find the electric field of this ‘atom’ at a distance $r$ ($r<a$) from the centre of the atom.

OR

A Dipole is made up of two charges $+q$ and $-q$ separated by a distance $2a$.

Derive an expression for the electric field $\vec{E}_e$ due to this dipole at a point distant $r$ from the centre of the dipole on the equatorial plane.

Draw the shape of the graph, between $|\vec{E}_e|$ and $r$ when $r>>a$.

If this dipole were to be put in a uniform external electric field $\vec{E}$, obtain an expression for the torque acting on the dipole.

25. State the law which relates to generation of induced emf in a conductor being moved in a magnetic field.

Apply this law to obtain an expression for the induced emf when one ‘rod’ of a rectangular conductor is free to move in a uniform, time independent and ‘normal’ magnetic field.

Apply the concept of the Lorentz (magnetic) force acting on a moving charge to justify the expression obtained above.

OR
An a.c. voltage \( V = V_m \sin \omega t \) is applied across an inductor of inductance \( L \).

Apply Kirchoff’s loop rule to obtain expressions for

(i) the current flowing in the circuit

(ii) the inductive reactance \( L \)

Hence find the instantaneous power \( P_i \) supplied to the inductor.

Show graphically the variation of \( P_i \) with \( \omega t \).

26. (a) Explain, with the help of a diagram, how is the phenomenon of total internal reflection used in

(i) an optical fibre

(ii) a prism that inverts an image without changing its size

(b) A right angled prism made from a material of refractive index \( \mu \) is kept in air. A ray PQ is incident normally on the side AB of the prism as shown.

Find (in terms of \( \mu \)) the maximum value of \( \theta \) upto which this incident ray necessarily undergoes total internal reflection at the face AC of the prism.

OR

State Huygen’s principle in wave-optics. How did Huygen ‘explain’ the absence of the backwave?
Use this principle to draw the refracted wave front for a plane wave incident from a denser to a rarer medium. Hence obtain Snell’s law of refraction.